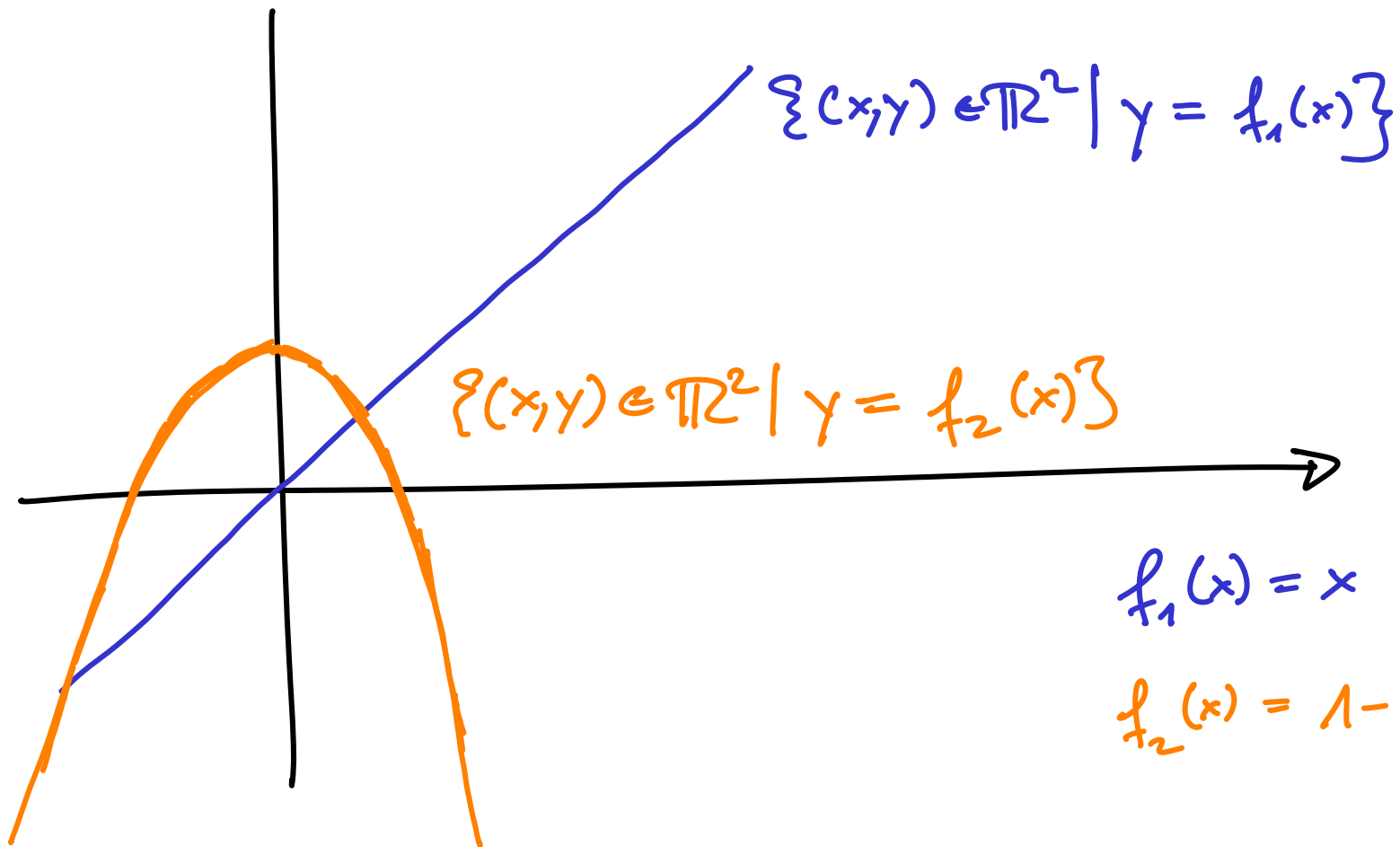


$$\{(x,y) \in \mathbb{R}^2 \mid x=2\}, \{(x,y) \in \mathbb{R}^2 \mid y=4\}, \{(x,y) \in \mathbb{R}^2 \mid x=y\}$$

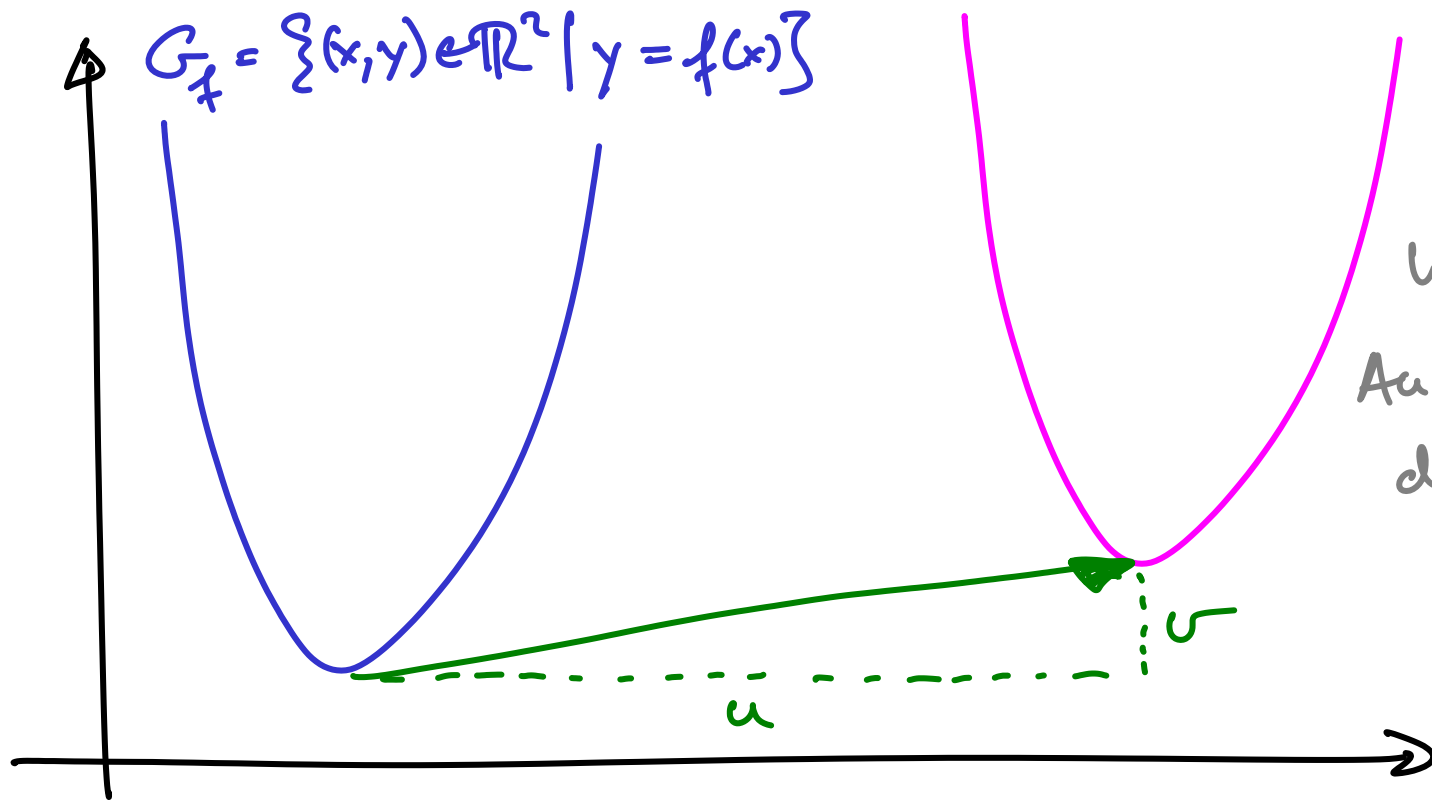
$$\{(x,y) \in \mathbb{R}^2 \mid x > 2\} \cap \{(x,y) \in \mathbb{R}^2 \mid y < 4\} \cap \{(x,y) \in \mathbb{R}^2 \mid y > x\}$$

$$= \{(x,y) \in \mathbb{R}^2 \mid x > 2 \text{ and } y < 4 \text{ and } y > x\}$$



$$f_1(x) = x$$

$$f_2(x) = 1 - x^2$$



Was ist g ?
Ausgedrückt
durch $f \dots$

$$G_f = \{(x, y) \in \mathbb{R}^2 \mid y = f(x)\}$$

$$\text{Translation: } (x, y) \mapsto (x+u, y+v) = (\tilde{x}, \tilde{y})$$

$$G_f \mapsto \{(x, y) \in \mathbb{R}^2 \mid y = f(x)\}$$

drückt durch (\tilde{x}, \tilde{y}) aus

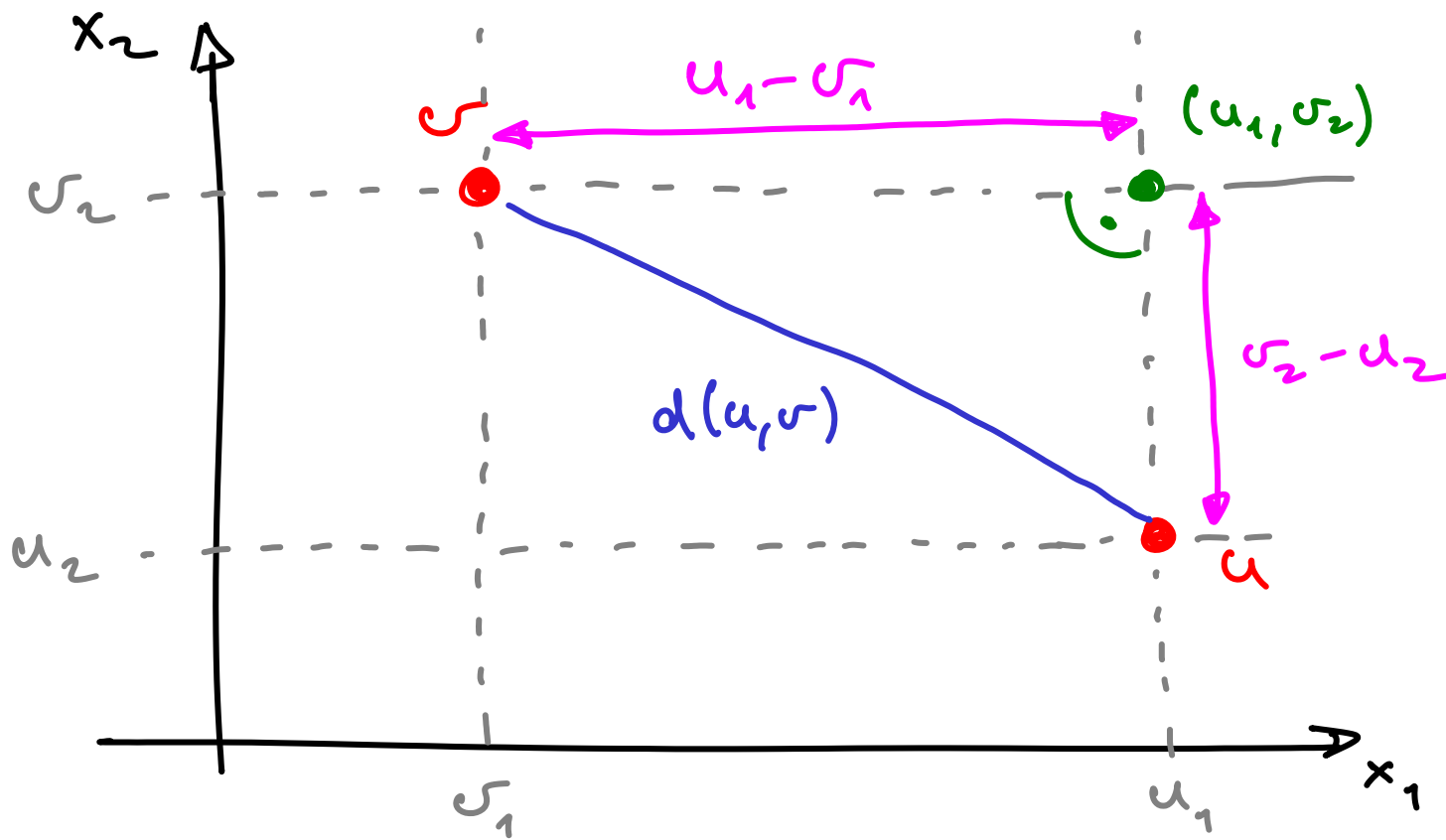
$$= \{(\hat{x}, \tilde{y}) \in \mathbb{R}^2 \mid \tilde{y} - v = f(\hat{x} - u)\}$$

$$= \{(\tilde{x}, \tilde{y}) \in \mathbb{R}^2 \mid \tilde{y} = f(\tilde{x} - u) + v\}$$

neu (\tilde{x}, \tilde{y})
alt (x, y)

$$= \{(x, y) \in \mathbb{R}^2 \mid y = f(x-u) + v\}$$

$$= G_g \quad \text{wobei} \quad g(x) = f(x-u) + v$$

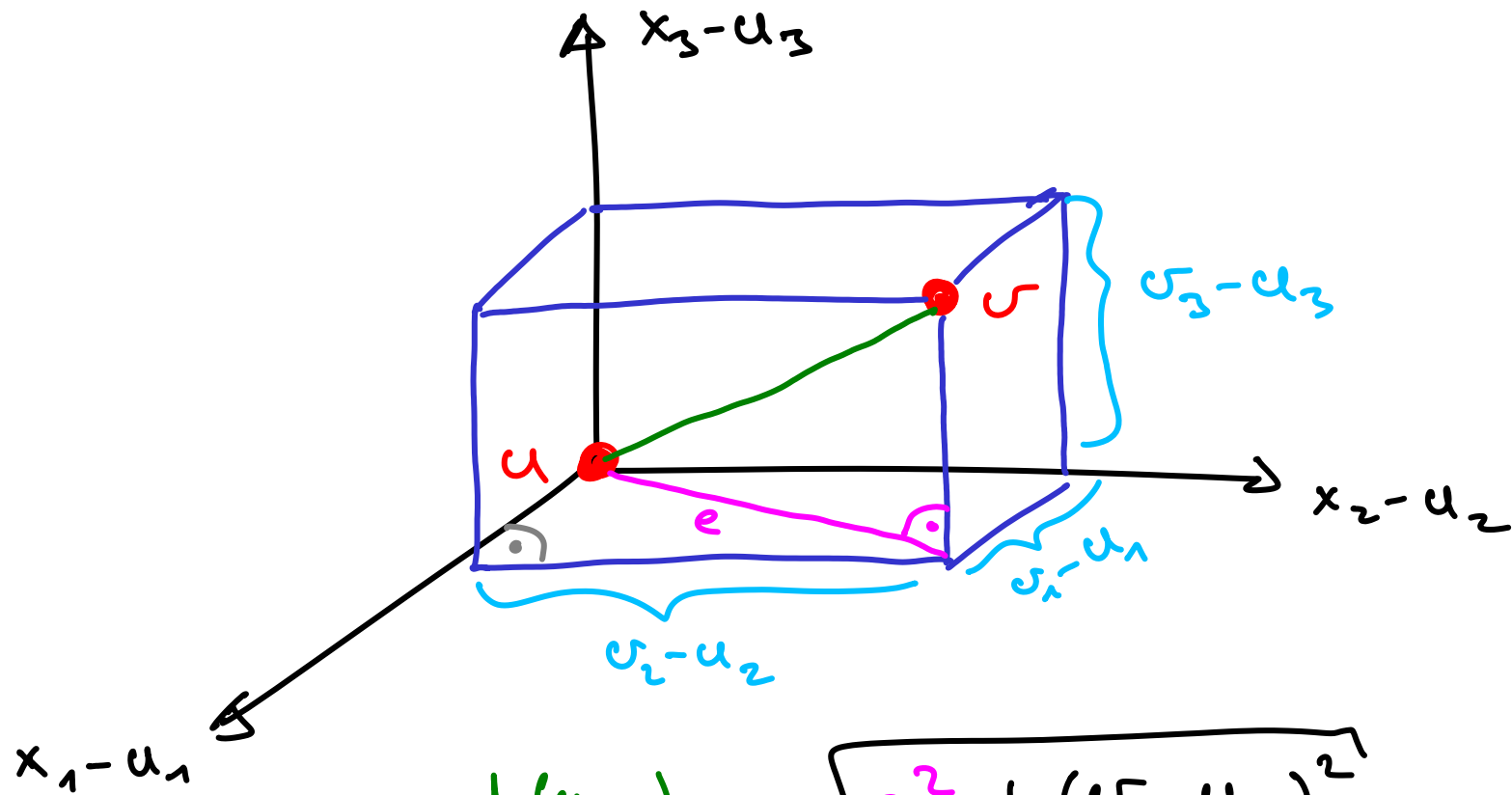


$$[d(u, v)]^2 = (v_1 - u_1)^2 + (v_2 - u_2)^2$$

$$\Rightarrow d(u, v) = \sqrt{(v_1 - u_1)^2 + (v_2 - u_2)^2}$$

$$d(u, v) = d(v, u), \quad d : \mathbb{R}^2 \times \mathbb{R}^2 \rightarrow \mathbb{R}$$

oder $d : \mathbb{R}^4 \rightarrow \mathbb{R}$



$$d(u, v) = \sqrt{e^2 + (v_3 - u_3)^2}$$

$$e^2 = (v_1 - u_1)^2 + (v_2 - u_2)^2$$

Erklärung für Bergmannsche Regel

Wärmeproduktion proportional zu Volumen V

Wärmeverlust proportional zur Oberfläche O

Quotient

$$\begin{array}{c} \nearrow \\ \text{Kragbar} \end{array} \frac{O}{V} \xrightarrow[\substack{(x,y,z) \mapsto (\alpha x, \alpha y, \alpha z) \\ \alpha > 1}]{\text{zentr. Streckung}} \underbrace{\frac{\alpha^2 O}{\alpha^3 V}}_{\text{Eisbar}} = \frac{O}{\underbrace{\alpha V}_{\nearrow \text{kleiner als} \\ \text{bzw. Kragbar}}}$$