Introduction to Commutative Algebra and algebraic Geometry Presence Exercise to Sheet 11

Exercise 1.

Let K be an algebraically closed field.

- a) Let $g \in K[x_1, \ldots, x_n]$. Prove: $\dim(D(g)) = n$.
- b) Let X be an irreducible affine variety in K^n and let $f \in \mathcal{O}(X)$, $f \neq 0$. Prove $\dim(X_f) = \dim(X)$. (Recall: $X_f = X \cap D(f)$.)