Introduction to Commutative Algebra and algebraic Geometry Presence Exercise to Sheet 9

Exercise 1.

Let K be an algebraically closed field. Determine the algebra of regular functions $O(U_i)$ for the following open sets U_i :

- $U_1 = K$,
- $U_2 = K \setminus \{0, 1\},$
- $U_3 = (X \setminus V(f)) \subset X$, where $X = V(x \cdot y \cdot z, x^2 xy^3) \subset K^3$ and $f = x^2 + y^2 + z^2 1 \in K[x, y, z]$.